

Fire Physics—Promises, Problems, and Progress

PATRICK J. PAGNI

Mechanical Engineering Department

University of California

Berkeley, California 94720, USA

ABSTRACT

The use of wanted fire leads necessarily to unwanted fires, which are fought by the fire services, designed against by the fire engineers, and observed and explained by the fire sciences. This paper explores the current position of one of those sciences - fire physics, defined as the study of the physical mechanisms by which fire is initiated, grows throughout a system, and is extinguished. The motivations for pursuing given technical areas are examined (promises), the tasks to be performed are described (problems) and the accomplishments to date are summarized (progress). The field of Fire Physics is broken into four broad categories: I.) Fluid Dynamics, II.) Diffusion Flames, III.) Flame Spread and IV.) Compartment Modeling. An inclusive list of topics within each category is presented. Space constraints prohibit a more comprehensive review, however reference is made to many competent reviews already available. Due to the author's linguistic limitations, the English language literature is emphasized.

HISTORY

It is interesting that anthropologists (1) now believe that the use of fire by homonids, i.e. by homo erectus c. 500,000 B.C. in Africa, precedes the evolution of the modern species of man, homo sapien. It is not clear when this use became controlled, i.e., when homonids could ignite fire at will rather than simply conserve it. At 10^6 B.C. it was not controlled; at 10^5 B.C. some evidence for control exists (2). The earliest artifacts indicating the ability to generate fire, flint and massive iron pyrite, date from 10^4 B.C. (3). In a few isolated existing societies ignition processes are unknown and the conservation of fire remains crucial (4). One of these groups, the Andaman Island people regard the possession of fire as the chief distinction between man and animal (5). The pyrolaters of ancient India addressed more hymns to the fire-god, Agni, than to any other pre-Hindu deity (6). During the European Middle Ages, flames were incorporated in heraldry (7). In existing societies the control of unwanted fire remains an important unresolved issue. The magnitude of the problem varies with the particular country (8,9). But all modern societies face the threat of destruction of life and property by escaped fire. Hence the need for fire science.

Several useful reviews of the history of fire science, particularly in the United States, are available (10) extending from pre-history (11)

to c. 2300 A.D. (12). U.S. activity prior to 1940 was centered in three locations: the National Fire Protection Association in Boston, the Underwriter's Laboratories in Chicago and the National Bureau of Standards in Washington. S.H. Ingberg's classic work in the 1920's addressed the question, How severe can fires be in buildings? An appropriate inquiry, since the primary problem of the time was to prevent the collapse of burned buildings onto adjacent structures or roadways (13). He observed and quantified the variation of fire duration and average room temperature with fuel load (14) thereby laying the empirical foundation for the standard furnace test time-temperature curve (15). Note that he obtained peak temperatures as high as 1050°C within 10 minutes of an "exposure start" with purely cellulosic fuels (see Fig. 6 of Ref. 14). This, primarily post-flashover, temperature history study is fire physics since the measurements were carefully made (with 100 thermocouples arrayed throughout the rooms) over a range of conditions (77 t $440 \text{ } 10^3 \text{ BTU/ft}^2$; $0.8 \text{ to } 5 \text{ MJ/m}^2$) and the author clearly stated his limitations and assumptions (14).

The National Academy of Sciences played a pivotal role in the 1950's and early 60's by forming the Committee on Fire Research with first H.C. Hottel and then H.W. Emmons as chair. That committee established the seminal journal Fire Research, Abstracts and Reviews, which later contained their recommendations for a fire research program (16) and Hottel's marvelously insightful analysis of Russian pool fire data (17), and published the first book on fire modeling (18).

The period from the late 60's to early 80's was particularly exciting, with the establishment of the Factory Mutual Research Corporation in Boston and the National Bureau of Standards Center for Fire Research in Gaithersburg, Maryland where the meeting founding the International Association for Fire Safety Science was held in October, 1985.

Parallel growth occurred, primarily independently, in several countries. The effort in the United Kingdom was focused at the Building Research Establishment's Fire Research Station begun in 1948 in Borehamwood. The progress of fire physics can be traced in the Information Papers, Fire Research Notes, journal articles and books (19, 20) authored by the FRS staff. Particularly noteworthy is the recent volume of selected papers by P.H. Thomas covering 35 years of fire physics scholarship from 1951 to 1986 (21). In Canada, the activities of the National Research Council's Division of Building Research predate those of the NBS Center for Fire Research. In Scotland, the University of Edinburgh's Unit of Fire Safety Engineering helped develop an outstanding text on fire physics (22). Australia has had a strong experimental program, including forest and brush fire control.

In Japan, several institutes, associations, and societies conducted fire physics research in this time frame. A major focus was at the Ministry of Construction's Building Research Institute first in Tokyo and now in Tsukuba. The initial progress there centered on experiments on wood cribs (23), room fires (24,25) and smoke generation (26) and on network analyses of smoke movement in buildings (27). The early work of Yokoi, Kawagoe, Saito, Wakamatsu and others, as recorded in the BRI Reports, Occasional Reports and Research Papers, laid the foundation for the current premier fire physics research position held by Japan, as evidenced by many excellent papers in the First and Second International Symposia on Fire Safety Science.

In Europe, Spain and Italy have been regular contributors to the Fire Research Colloquia at the Combustion Institute's biennial International Symposia on Combustion (28). Important fire physics contributions have come from Sweden (Lund Institute of Technology, National Testing Institute, and Fire Protection Association); Germany (Technische Universität Braunschweig, Universität Karlsruhe; and Gesamthochschule Kassel Universität); France (Université de Poitiers and Centre Scientifique et Technique du Bâtiment); Denmark (Technical University); Norway (Fire Research Laboratory) and others.

Table 1. FIRE PHYSICS

I. FLUID DYNAMICS

1. Buoyant Flames and Plumes
 Flow Regimes
 Transition Criteria
 Near Field
 Velocity and
 Temperature Profiles
 Far Field
 Entrainment Rates
 Coherent Structures
 and Other Oscillations
 Droplet Dynamics
 Interactions with Walls,
 Ceilings, Layers and Flows
 Reaction Distributions
 Flame Base Field
2. Flows Within Compartments
 Ceiling Layer Formation
 Two-Layer Temperatures
 Extended Fire Plumes
 Ceiling Jets
 Stratification
 Corridors
 Mixing
3. Flows at Openings
 Doors
 Windows
 Ceiling Holes
 Multiple Openings
 HVAC Systems
 Mixing
4. Nondimensionalization

II. DIFFUSION FLAMES

1. Pyrolysis Rates Flame Shapes
 Laminar Boundary Layers
 Free, Forced and Mixed
 Burning distinct
 from Pyrolyzing
 Heat Release Rate Databases
 Turbulent Boundary Layers
 Free, Forced and Mixed
 Radiant Augmentation
 Blockage Effects
 Liquid and Solid Pools
 Walls, Ceilings and Corners
 Cribs, Carpets and Furniture
 Charring
 Melting
2. Excess Pyrolyzate
 Production
 Composition
 Accumulation and
 Flammability Limits
3. Flame Radiation
 Temperature, Geometry
 and Composition Effects
 Heat Release Rate Fraction
 Wavelength Dependence
 Soot as % of Fuel Carbon
 Soot Volume Fraction
 Measurement
 Correlations
 Analyses
4. Nondimensionalization

III. FLAME SPREAD

1. On Solids/Liquids
 - Laminar/Turbulent
 - Thick/Thin
 - Up/Down Vertical Walls
 - Opposed/Assisted Flow
 - Horizontal
 - Surface Tension Effects
 - Transport Mechanisms
 - Radiant Augmentation
 - Oxygen Variation
 - Correlations
 - Damköhler No.
 - Empirical
 - Ignition Temperature
 - Ignition Phenomena
 - Remote Object
 - Piloted/Fire Brand
 - Extinction Phenomena
 - Melting
 - Charring
 - Critical Kinetics-Gas/Solid
2. In Solids (Smoldering)
 - Porous Media Flow
 - Heat and Mass Transport
 - Counter-Current (Diffusion)
 - Co-Current (Premixed)
 - Self-heating to Ignition
 - Surface Reactions
3. In Gases
 - Deflagrations/Detonations
 - Confined/Unconfined
 - Pure Mixtures
 - Vitiated Mixtures
 - Ceiling Layer Limits
 - and Propagation Speeds
 - Ignition/Extinction
 - Stratification
4. Growth Models
 - Exponential/Power Law
 - Doubling Time
 - Smoke Movement
 - Fire Growth Rate Parameter
 - Growth Classification
 - Intensity Classification
 - Threat Variables
 - Escape Time
5. Nondimensionalization

IV. COMPARTMENT MODELING

1. Heat Transfer
 - Conduction Losses
 - Thermal Inertia
 - Convection Losses
 - Convection Between Layers
 - Flame Impingement
 - Smoke Layer
 - Visibility
 - Radiation
 - Surface Radiant Exchange
 - Accurately Described
 - Approximations
 - Radiation Rate Pool
2. Pyrolysis and Burning Rates
 - Ventilation Control
 - Vitiation
 - Radiative Feedback
3. Growth to Flashover
 - Ventilation
 - Free, Forced, None
 - Pressure
 - Characteristic Times
 - Temperature Field History
 - Species Field History
 - Computation
 - Zone
 - Field
 - Scale Effects
 - Stratification
 - Oscillations
4. Flashover
 - Definitions
 - Criteria
 - Approximations
 - Stability Analyses
 - Windows Breaking
 - Venting
 - Backdrafts
 - Air Flames
5. Fire Spread to Adjacent Spa
 - Postflashover Intensity
 - Flame Heights Out Windows
 - Flame Propagation and Leng
 - along Adjacent Ceilings
 - Multiple Rooms
6. Nondimensionalization

PROMISES

The session titles at this symposium could serve to identify the branches of fire science. Of interest here is fire physics which can be defined as the study of the physical mechanisms by which fire is initiated, grows and is extinguished. Our goal is to provide life safety from fire by understanding the physics of fire sufficiently to develop mathematical models or empirical correlations which predict the evolution of any fire and, based on these predictions, to suggest test methods or standards which will properly identify fire hazards. The boundaries between fire physics and the other branches of fire science, especially fire chemistry, are blurred and listing problems here does not imply exclusivity but rather partnership, with each area contributing its expertise to the solution of an appropriate sub-problem. Solving complex problems will require cooperation and appreciation, rather than competition, among disciplines.

The promise is basically the same across the fire sciences, i.e., that there exist bodies of fundamental knowledge accrued by science over time which can be applied, directly or with a few small steps advancing the frontiers, to the solution of fire problems. This knowledge is available in universities, industries and government laboratories throughout the world. All that is required is the insight to see and the energy to make the needed connections between the right fundamentals and the fire-related applications. In fire physics, the period 1980-2010 A.D. appears ripe for forging these connections. The fundamental disciplines: fluid mechanics, thermodynamics, transport mechanics, etc., are mature. The required computational power is becoming available. The time for action is now.

PROBLEMS

Table 1 is an attempt to organize the fields within fire physics and to inclusively list all pertinent phenomena. The order is from best to least understood, or in the case of the four main divisions, from most to least mature. Each problem is listed only once, at its first appearance, since its solution is assumed to be available where required further down the table, e.g., "ceiling layer formation" appears under Fluid Dynamics and is not repeated in Compartment Modeling. This concise synthesis can not claim uniqueness and claiming completeness would be rash. But, at the least, Table 1 should have usefulness as a springboard for productive debate. There exist many interconnections among these problems which a one-dimensional list can not display. An appropriate project for the future would be to develop a multi-dimensional Hasemi Diagram (29) or Lighthill Map (30) for fire physics. The individual problems are discussed in the following progress section. Less emphasis than might be expected is placed on future work since that was so well described in the First Symposium invited lecture on fire physics (31). The 141 references cited there are a veritable gold mine of fire physics information. Nondimensionalization is listed at the end of each main division because it does not appear to have yet received the explicit attention it merits. It has been suggested, perhaps incorrectly, that in developing a large precision code (12) for calculating the evolution of a compartment fire, nondimensionalization may not have great utility. However, in practical codes (12), in simplified correlations (32) and in attempts to scale fire phenomena (33,34), identifying the optimum dimensionless groups will be the key problem, just as in the more fundamental branches of physics.

I. Fluid Dynamics

1. Buoyant Flames and Plumes. This section uses Table 1 as an outline, highlighting available conclusions and noting areas where further efforts are needed. The references cited are examples, meant to provide entry points to the literature in each area. The Emmons Lecture of the First Symposium is required reading in the field of fire fluid dynamics (35). Buoyant flames and plumes are well covered in the other invited fire physics lecture in this symposium (36). Zukoski (35) has identified the governing dimensionless group for large diffusion flames as the enthalpy generation scaled by the buoyant convection of enthalpy, i.e.,

$$Q^* \equiv \dot{Q} / (\rho_{\infty} c_{p\infty} T_{\infty} g^{1/2} D^{5/2}) \quad (1)$$

where \dot{Q} is the total heat release rate, D is the fire base diameter, g is 9.8 m/s^2 , and ρ_{∞} , $c_{p\infty}$ and T_{∞} are the gas density, specific heat capacity, and temperature at ambience. Three flow regimes and two transition regimes have been identified. Transition (IV) to a momentum dominated regime (V) occurs for $Q^* \gtrsim 10^3$. In the range, $1 \lesssim Q^* < 10^3$, the flow is buoyancy dominated (III) and the flame height, at 50% intermittency, in units of the base diameter, is

$$Z_f/D \approx 3.3 Q^{*2/5} \quad (2)$$

Equation (2) shows that the flame height is independent of the base diameter, as expected for large turbulent buoyant flames where the fuel flow rate, not the diameter, matters. Note that Q^* decreases as D increases and as Q^* approaches unity, the pulsation normally observed at the flame base grows into strong oscillations (37) initiating the transition (II) to a regime (I), $Q^* \lesssim 0.1$, where the flame column has broken into a ring of separate flamelets.

The adiabatic plume above the fire, or far field, is well understood (38,39) provided the actual distributed enthalpy source can be modeled as a point source. The virtual origin is the device usually chosen to accomplish this (40-42). Let Z_0 be the height of the origin above the flame base, then

$$Z_0/D \approx 0.33 (2 - Z_f/D) \quad (3)$$

correlates most data (35) giving a virtual origin below the base for tall flames, $Z_f/D > 2$, and above for short flames. Modern mathematical methods are being applied to the whole flow field (43). But for now entrainment rate data (39,42) continue to be useful. Ingenious temperature and velocity field measurements have also been made (44-46). But analyses of reacting flows in these geometries remain undone. Also areas for fruitful future activity are droplet dynamics (47,48) and plume interactions (49,50).

2. Flows Within Compartments and 3. Flows at Openings. The previous section addressed unenclosed plumes and flames. Here confinement, with holes, is added. Zukoski (35,51) explains the formation of two layers, the upper hot and lower cold, in a compartment fire. Stratification is reduced by the recirculation of the hot gas in the upper layer due to entrainment or re-entrainment in the plume and ceiling jet and due to the circular flow path produced by walls and buoyant forces. The soffit or intrados of doors and windows also cause outgassing of the

intermediate temperature material (see Figs. 1 and 10, ref. 35). The history of the two-layer model has been reviewed by Quintiere (52). Both authors (35,52) discuss conditions under which stratifications occur. The unsteady growth to the two-layer condition has been examined (53,54) as have the flows within the ceiling layer (49,55-57). Flow in corridors (31,35,35) and mixing are areas under current study.

Vertical vents, i.e., windows, doors, holes, can be treated as orifices using standard methods (24,31,35) with an orifice coefficient of 0.7 (35,58), within ~ 10%. Horizontal vents are more difficult since both buoyancy and pressure effects can be important producing inherently unsteady flows, but preliminary studies (31,35,59) are available. Some work has been done on forced flow systems (60,61) and multiple openings (62). Further discussion of room fire fluid dynamics is more appropriate under Compartment Modeling.

Table 2. General Results for Diffusion Flame Species and Enthalpy Fields

	$< \eta_{fl}$	η_{fl}	$> \eta_{fl}$
$Y'_o \equiv Y_o/Y_{o\infty}$	0	0	$1-(1+\phi)J$
$Y'_f \equiv Y_f/Y_{fw}$	$(1+1/\phi)J-1/\phi$	0	0
$h' \equiv h/Q_o Y_{o\infty}$	$1-(1-h'_w)J$	$(h'_w+\phi)/(1+\phi)$	$(h'_w+\phi)J$
$Y'_p \equiv (Y_p - Y_{p\infty})/Y_{o\infty}(1+s)$	$1-(1-Y'_{pw})J$	$(Y'_{pw} + \phi)/(1+\phi)$	$(Y'_{pw} + \phi)J$
$Y'_n \equiv Y_n/Y_{n\infty}$	$1-(1-Y'_{nw})J$	$(Y'_{nw} + \phi)/(1+\phi)$	$1-(1-Y'_{nw})J$

Notes: $< \eta_{fl}$ indicates the fuel side of the reactant sheet and $> \eta_{fl}$ indicates the oxidant side. Y_i is the species mass fraction, h is gas enthalpy relative to ambient, Q_o is ~ 13 kJ/gm of O_2 , s is the stoichiometric ratio $\nu_f M_f / \nu_o M_o$, $\phi \equiv Y_{fw}/Y_{o\infty}s$ is the diffusion flame equivalence ratio and

$$J \equiv \frac{\left[\frac{Y_f}{\nu_f M_f} - \frac{(Y_o - Y_{o\infty})}{\nu_o M_o} \right]}{\left[\frac{Y_{fw}}{\nu_f M_f} + \frac{Y_{o\infty}}{\nu_o M_o} \right]} \equiv \frac{\left[h + \frac{(Y_o - Y_{o\infty})}{\nu_o M_o} \right]}{\left[\frac{h_w}{Q} - \frac{Y_{o\infty}}{\nu_o M_o} \right]} \equiv \frac{\left[\frac{(Y_p - Y_{p\infty})}{\nu_f M_f + \nu_o M_o} + \frac{(Y_o - Y_{o\infty})}{\nu_o M_o} \right]}{\left[\frac{(Y_{pw} - Y_{p\infty})}{\nu_f M_f + \nu_o M_o} - \frac{Y_{o\infty}}{\nu_o M_o} \right]} \equiv \frac{Y_n - Y_{n\infty}}{Y_{nw} - Y_{n\infty}}$$

is the normalized conserved Shvab-Zeldovich variable. The subscripts are: f = fuel, fl = flame, n = inert, o = oxygen, p = product, r = fuel reservoir, w = reservoir surface, and ∞ = ambient. Assuming the reservoir surface enthalpy, h_w , is known, it has been shown (66) that $Y_{fw} = (BY_{fr} - sY_{o\infty})/(1+B)$, $Y_{pw} = (Y_{p\infty} + (1+s)Y_{o\infty})/(1+B)$ and $Y_{nw} = (BY_{nr} + Y_{n\infty})/(1+B)$ where $B \equiv (Q_o Y_{o\infty} - h_w)/L$, with L the effective latent heat of pyrolysis, is Spalding's mass transfer number (73).

II. Diffusion Flames

1. Pyrolysis Rates/Flame Shapes and 2. Excess Pyrolyzate. Adding reactions explicitly to the fluid mechanics leads to the field of combustion and gives access to the classic studies of reacting boundary layers (63-65). Several reviews are available (66-68). Laminar systems are well understood and serve to identify the parameters important to systems in which energy feedback from the flame provides pyrolysis products for burning. Table 2 gives the enthalpy and species fields in any system to which the fast kinetics Shvab-Zeldovich assumptions (69) apply. Extensions exist to include radiation (70,71) and multiple flame sheets (71,72). These results also supply the far field for applying activation-energy asymptotics (69) to incorporate finite rate kinetics in diffusion flame analyses. Species and temperature fields are obtained from Table 2 by solving the appropriate conservation equations and boundary conditions for $J(\eta)$ (66).

The key dimensionless group is the diffusion flame equivalence ratio,

$$\phi = Y_{fW}/Y_{O_{\infty}S} \quad (4)$$

where the notation is defined in the notes to Table 2. The equivalence ratio has long been a useful measure of fuel richness associated with premixed flames (69). ϕ emerges here as also applicable to diffusion flames and the richer the flame, the greater the hazard. Table 3 shows the effects of chemical properties on flame heights, $x_{f\ell}$, normalized to the pyrolyzing fuel height, λ (66). A free flame length of 2.4 for cellulose means that the flame exists 1.4 λ above the fuel, as typically observed for a fireplace log. Polyurethane produces flames three times as long as cellulose and thereby presents a greater fire spread hazard.

Low stoichiometric ratios, s , and latent heats of pyrolysis, L , produce high surface fuel mass fractions, Y_{fW} , and high equivalence ratios, ϕ . High ϕ means much fuel is being generated which must reach out to find the oxygen required to burn. Hence high ϕ 's correspond to long flames which travel along ceilings, out doors and down corridors spreading the fire as they go. Alternatively, in closed systems, at high

Table 3. Flame extensions and properties for foam polymers (74,75)						
Material	s	L(kJ/g)	B	Y_{fW}	ϕ	$x_{f\ell}/\lambda$
Polystyrene, GM-49 $C_8H_{8.4}O_{0.03}$	0.33	1.3	1.7	0.6	8.3	12.0
Polyurethane, GM-25 $C_{3.1}H_{5.4}ON_{0.22}$	0.46	1.2	1.5	0.6	5.3	7.5
Polyisocyanurate, GM-41 $C_{5.3}H_{5.2}ON_{0.57}$	0.43	4.5	0.4	0.2	2.3	2.8
Cellulose, filter paper $C_6H_{10}O_5$	0.84	3.5	0.8	0.3	1.7	2.4

ϕ much fuel is being pyrolyzed which is not being burnt. That fuel has been called excess pyrolyzate (76). As the excess pyrolyzate accumulates, combustible mixtures form which can lead to rapid gas phase fire spread once venting occurs (77,78). While the results in Table 3 are from laminar calculations (66,79), the same relative ranking persists for turbulent systems (80,81) which have shorter flames (82) and are dominated by radiation (83,84).

A considerable literature on pool fires is available (37,67,85-88). Substantial heat release rate databases are being produced by Babrauskas of the NBS Center for Fire Research (89-91) and by Tewarson at Factory Mutual Research Corporation (74,92). Descriptions of pyrolysis rates and flame shapes for practical systems are listed under Fire in the cumulative subject indices of the International Symposia on Combustion (93,94).

3. Flame Radiation is recognized as the dominant energy transport mechanism in full scale fires (95,96). The emergence of radiation with increasing scale, over the convection dominant at small scale, prohibits scaling fire phenomena from bench top to real size. The fundamental influences of temperature, geometry and composition are well known (97-99). Efficient application to practical fires is the problem. Orloff (87) suggests an effective radiation flame temperature of 1260 K for small pool fires. The mean beam length approach appears to suffice for physical path calculations (95-97) and soot is the primary radiator (95-99). Non-homogenities in the temperature and species fields may be important (86,87,99-101). A useful simplification has been to express the flame radiation as a fraction of the heat release rate, $\sim 1/3$, (95,100) and assume isotropy. Tien and co-workers have examined the spectral distribution of flame radiation (96) and its absorption by pyrolyzate (101).

Since the wavelengths of infrared flame emission are large ($\sim 3 \mu\text{m}$), compared with the circumferences of most soot particles ($\lesssim 0.3 \mu\text{m}$), absorption dominates scattering and the detailed soot size distribution does not affect flame radiation. It is only necessary to know the soot volume fraction, f_v , i.e., the fraction of the flame volume occupied by soot. The soot volume fraction is $\sim 10^{-6}$ (95-105), which corresponds to the conversion of $\sim 5\%$ of the pyrolyzed fuel carbon to soot (104). The soot emissivity (96,104) can be approximated by

$$\epsilon_s = 1 - \exp(-\kappa L), \quad (5)$$

where L is the flame mean beam length and the effective soot absorption coefficient is

$$\kappa \approx 1.27 \times 10^3 f_v T_f, \quad (\text{m}^{-1} \text{ for } T_f \text{ in K}). \quad (6)$$

It has been suggested that for pool fires, the soot volume fraction scales with optical path as

$$f_v / f_{v \text{ max}} \approx 1.5 (\kappa L)^{1/3}, \quad \text{for } \kappa L < 0.3. \quad (7)$$

For $\kappa L \geq 0.3$, $f_v = f_{v \text{ max}}$, a fuel property determined experimentally to range from ~ 0.2 ppm for ethanol and ~ 0.6 ppm for wood to ~ 0.9 ppm for polyurethane and ~ 4 ppm for polystyrene (104). Several diagnostic techniques are available to measure f_v in situ (102,103), but the unraveling of the mechanism of soot formation remains one of the great unsolved combustion problems (102,105).

A thorough review of each of these divisions could easily occupy all 15 allowed pages. But my allotment is already exceeded, so I will only cite a few reviews for flame spread (20,69,77,93,94,106-117) and compartment modeling (14,21,24,32,51-62,118-130) and carry forward one thread from the fire physics invited lecture at the last symposium. Professor Emmons identified window breaking as a key unresolved problem (31) and gave, in his usual way, sufficient physical insight to make a solution tractable. A window breaks in a fire for the same reason that an ice cube cracks when placed in liquid. Thermal expansion places the cooler portion in tension. The exposed window heats and expands placing its cooler shaded edge in tension until it cracks at a small defect, usually at the top inner edge. The pressure difference across the window is sufficient to remove it within milliseconds after the crack is initiated. Glass can only stand a small tensile stress, $\sigma \sim 4 \times 10^7 \text{ N/m}^2$ ($\sim 6000 \text{ psi}$) (131). The stretch modulus for glass is $E = 7.8 \times 10^{10} \text{ N/m}^2$ ($1.1 \times 10^7 \text{ psi}$) (132). So the strain, $\epsilon = \sigma/E$, required to crack the glass is $\sim 0.05\%$. The temperature rise needed to produce that strain is $\Delta T = \epsilon/\alpha \approx 58^\circ\text{C}$ (104°F), since the coefficient of linear thermal expansion for glass is $\alpha \approx 9.2 \times 10^{-6} \text{ }^\circ\text{C}^{-1}$ ($5.1 \times 10^{-6} \text{ }^\circ\text{F}^{-1}$) (132). My fracture mechanics colleagues at Berkeley ran the two-dimensional, unsteady version of this problem (133) on the Cray computer and got $\Delta T = 60^\circ\text{C}$ (108°F) for the same property values. The 2°C increase in the window temperature rise at fracture is due to conduction into the cooler edge region. These results appear to be independent of scale. So compartment modelers may assume windows act as vents after the glass reaches $\sim 80^\circ\text{C}$. The energy transport between flame, smoke layer and glass remains to be modeled.

CONCLUSION

An in-depth review of fire physics as originally envisioned requires a book rather than an article. And like the painting of our Bay Bridge, the book would take sufficiently long to write, that it would be necessary to start all over again when it was finished. What a delightful position for a researcher to be in.

Much has been accomplished in fire physics. Our long range goals are clear (12,29,31). Our short range goals should include better communication with our colleagues - both those on the practical side who bear the responsibility for implementing these results as improved test methods and codes and those on the fundamental side whose expertise we need to advance the frontiers of fire physics. It may be that the problems are too complex, too dependent on detail, too terrible in their physical and legal consequences, to allow us to succeed in the short term in replacing specification codes with performance codes. Perhaps we need to be content with smaller goals such as suggesting improvements in current designs and standards. One appropriate step is to apply what is now known to model accidental fires after they have occurred to reconstruct the details and thus identify fruitful directions for future research (78,134).

ACKNOWLEDGEMENTS

The support of the U.S.D.O.C. National Bureau of Standards - Center for Fire Research under Grant 60NANB5D0552 is most appreciated. The author apologizes to those authors who should have been included in this review, but were not, due to the author's ignorance and the editors' length restrictions.

REFERENCES

1. Clark, J.D., and Harris, J.W.K., "Fire and its Roles in Early Hominid Lifeways," The African Archeological Review, 3, 3-27, 1985.
2. Barbetti, M., Clark, J.D., Williams, F.M., and Williams, M.A.J., "Paleomagnetism and the Search for Very Ancient Fire Places in Africa," Anthropologie, 18:2, 299-304, 1980.
3. Perles, C., "Ré-examen Typologique de l'Industrie du Ponc Epic (Ethiopie): les Pointes et Pièces Pointues," L'Anthropologie 78, 529-552, 1974.
4. Radcliffe-Brown, A.R., The Andaman Islanders, p. 201, New York, 1964.
5. Ibid. p. 258.
6. Funk & Wagnalls New Encyclopedia, 10, p. 206, Funk & Wagnalls, New York, 1983.
7. Di Crollanza, G.B., Dizionario Storico-Blasonico delle Famiglie Nobili e Notabili Italiane, 3, p. 272, Arnaldo Forni, Bologna, 1965.
8. Lyons, J.W., Fire, p. 4, W.H. Freeman, New York, 1985.
9. Wilmot, T., "National Fire Costs - A Wasteful Past but a Better Future," in Fire Safety Science-Proceedings of the First International Symposium, eds. C.E. Grant and P.J. Pagni, 1009-1018, Hemisphere, New York, 1986.
10. Hottel, H.C., "Stimulation of Fire Research in the United States after 1940 (A Historical Account)," in Fire Science for Fire Safety, eds. R.S. Levine and P.J. Pagni, 1-10, Gordon and Breach, London, 1984.
11. Emmons, H.W., "The Growth of Fire Science," Fire Safety J., 3, 95-106, 1980/81 (Special Issue Dedicated to P.H. Thomas).
12. Emmons, H.W., "The Further History of Fire Science" in Fire Science for Fire Safety, eds. R.S. Levine and P.J. Pagni, 499-506, Gordon and Breach, London, 1984.
13. Robertson, A.F., "Simon H. Ingberg - NBS Pioneer in Fire Research," privately communicated on the 100th anniversary of Ingberg's birth, 24 June 1977.
14. Ingberg, S.H., "Tests of the Severity of Building Fires," National Fire Protection Association Quarterly, 22:1, 43-61, 1928.
15. ASTM, "Standard Method of Fire Tests of Building Construction and Material," in Annual Book of ASTM Standards, 04.07, 349-375, Philadelphia, 1985.
16. National Academy of Sciences - National Research Council Committee on Fire Research, "A Proposed Fire Program", Fire Research Abstracts and Reviews, 1:1, 1-8, 1958.

17. Hottel, H.C., "A Review of 'Certain Laws Governing Diffusive Burnin of Liquids' by V.I. Blinov and G.N. Khudiakov," Fire Research Abstracts and Reviews, 1:2, 41-44, 1959.
18. Use of Models in Fire Research, NAS-NRC Publication No. 786, 1961.
19. Palmer, K.N., Dust Explosions and Fires, Chapman and Hall, London, 1973.
20. Bowes, P.C., Self-heating: Evaluating and Controlling the Hazards, Building Research Establishment, HMSO Books, London, 1984.
21. Thomas, P.H., Selected Papers, 1951-1986, Fire Research Station, Building Research Establishment, HMSO Books, London, 1986.
22. Drysdale, D., An Introduction to Fire Dynamics, John Wiley and Sons New York, 1985.
23. Yokoi, S., "On the Heights of Flames from Burning Cribs," BRI Occasional Report No. 12, Ministry of Construction, Tokyo, 1963.
24. Kawagoe, K., "Fire Behavior in Room Fires," BRI Report No. 27, Ministry of Construction, Tokyo, 1958.
25. Kawagoe, K., "Estimation of Fire Temperature - Time Curve in Rooms, BRI Research Paper No. 29, Ministry of Construction, Tokyo, 1967.
26. Saito, F., "Study on Smoke Generation from Building Materials," BRI Research Paper No. 33, Ministry of Construction, Tokyo, 1968.
27. Wakamatsu, T., "Calculation of Smoke Movement in Buildings," BRI Research Papers No. 34 (First Report) and No. 46 (Second Report), Ministry of Construction, Tokyo, 1968 and 1971.
28. Proceedings of the Tenth and following International Symposia on Combustion, The Combustion Institute, Pittsburgh, 1965 et seq.
29. Proceedings of the United States-Japan National Resources Panel Meetings on Fire Research and Safety, BRI - Tsukuba and NBS - Gaithersburg, 1974 et seq.
30. Lighthill, M.J., "Waves in Fluids," Comm. on Pure and Appl. Math., 20:2, 267-293, 1967.
31. Emmons, H.W., "The Needed Fire Science," in Fire Safety Science - Proceedings of the First International Symposium, eds. C.E. Grant and P.J. Pagni, 33-53, Hemisphere, New York, 1986.
32. Lawson, J.R., and Quintiere, J.G., "Slide Rule Estimates of Fire Growth," Fire Tech. 21:4, 267-292, 1985.
33. Williams, F.A., "Scaling Mass Fires," Fire Research Abstracts and Reviews 11:1, 1-23, 1969.
34. Quintiere, J.G., McCaffrey, B.J., and Kashiwagi, T., "A Scaling Study of a Corridor Subject to a Room Fire," Comb. Sci. and Tech. 18:4, 1-19, 1978.

35. Zukoski, E.E., "Fluid Dynamic Aspects of Room Fires," in Fire Safety Science - Proceedings of the First International Symposium, eds., C.E. Grant and P.J. Pagni, 1-30, Hemisphere, New York, 1986.
36. Baum, H.R., and McCaffrey, B.J., "Fire Plume Flow Fields, Theory and Experiment" this Symposium.
37. Weckman, E.J., "The Structure of the Flow Field Near the Base of a Medium-Scale Pool Fire," doctoral dissertation, Mechanical Engineering, University of Waterloo, Ontario, Canada, 1987.
38. Morton, B.R., Taylor, G.I., and Turner, J.S., "Turbulent Gravitational Convection from Maintained and Instantaneous Sources," Proc. Roy. Soc. London, A234, 1-23, 1956.
39. Cetegen, B.M., Zukoski, E.E., and Kubota, T., "Entrainment in the Near and Far Field of Fire Plumes," Comb. Sci. and Tech., 37, 305-331, 1984.
40. Heskestad, G., "Virtual Origins of Fire Plumes," Fire Safety J., 5:2, 109-114, 1983.
41. Kung, H., and Stavrianidis, P., "Buoyant Plumes of Large-Scale Pool Fires," 19th Int'l. Symp. on Comb., 905-912, The Combustion Institute, 1982.
42. Zukoski, E.E., Kubota, T., and Cetegen, B.M., "Entrainment in Fire Plumes," Fire Safety, J., 3, 107-121, 1980/81.
43. Baum, H.R., R.S. Springer Professorship Lectures, Mechanical Engineering, University of California at Berkeley, 1984.
44. McCaffrey, B.J., "Purely Buoyant Diffusion Flames: Some Experimental Results," NBSIR 79-1910, NBS, Washington, 1979.
45. Delichatsios, M., and Orloff, L., "Entrainment Measurements in Turbulent Buoyant Jet Flames and Implications for Modeling," 20th Int'l. Symp. on Comb., 367-375, The Combustion Institute, 1984.
46. Tamanini, F., "Direct Measurements of Longitudinal Variation of Burning Rate and Product Yield in Turbulent Diffusion Flames," Comb. and Flame, 51, 231-243, 1983.
47. Yuen, M.C., and Chen, L.W., "On Drag of Evaporating Droplets," Comb. Sci. and Tech., 14, 147-154, 1976.
48. Alpert, R.L., "Calculated Interaction of Sprays with Large-Scale Buoyant Flows," ASME J. Heat Transfer, 106:2, 310-317, 1984.
49. Alpert, R.L., "Turbulent Ceiling Jet Induced by Large Scale Fires," Comb. Sci. and Tech., 11, 197-213, 1975.
50. Cooper, L., "On the Significance of a Wall Effect in Enclosures with Growing Fires," Comb. Sci. and Tech., 40, 19-36, 1984.
51. Zukoski, E.E., and Kubata, T., "Two-Layer Modeling of Smoke Movement in Building Fires," Fire and Materials, 4:1, 17-21, 1980.

52. Quintiere, J.G., "A Perspective on Compartment Fire Growth," in Fire Science for Fire Safety, eds. R.S. Levine and P.J. Pagni, 11-54, Gordon and Breach, London, 1984.
53. Zukoski, E.E., "Development of a Stratified Ceiling Layer in the Ear Stages of a Closed-Room Fire," Fire and Materials, 2:2, 54-62, 1978.
54. Walton, W.D., "ASET-B: A Room Fire Program for Personal Computers," Fire Tech., 21:4, 293-311, 1985.
55. You, H.Z., and Faeth, G.M., "Ceiling Heat Transfer During Fire Plume and Fire Impingement," Fire and Materials, 3, 140-147, 1979.
56. Cooper, L.Y., "Convective Heat Transfer to Ceilings Above Enclosure Fires," 19th Int'l. Symp. on Comb., 933-939, The Combustion Institute, 1982.
57. Evans, D.D., "Calculating Fire Plume Characteristics in a Two-Layer Environment," Fire Tech., 20:3, 39-63, 1984.
58. Steckler, K.D., Baum, H.R., and Quintiere, J.G., "Fire Induced Flows Through Room Openings-Flow Coefficients," 20th Int'l. Symp. on Comb. 1591-1600, The Combustion Institute, 1984.
59. Emmons, H.W., "The Ingestion of Flames and Fire Gases into a Hole in an Aircraft Cabin for Arbitrary Tilt Angles and Wind Speeds," Harvar Home Fire Project Report 52, Cambridge, 1982.
60. Mitler, H.E., "Zone Modeling of Forced Ventilation Fires," in Fire Science for Fire Safety, eds. R.S. Levine and P.J. Pagni, 83-106, Gordon and Breach, London, 1984.
61. Pagni, P.J., Alvares, N.J., and Foote, K.L., "Defining Characteristic Times in Forced Ventilation Enclosure Fires," in Mathematical Modeling of Fire, STP 983, ed. J.R. Mehaffey, 68-82, ASTM, Philadelphia, 1987
62. Tanaka, T., "A Model of Multiroom Fire Spread," NBSIR 83-2718, NBS, Washington, 1983.
63. Emmons, H.W., "The Film Combustion of Liquid Fuel," Z. Math. und Mec 36:1/2, 60-71, 1956.
64. Burke, S.P. and Schumann, T.E.W., "Diffusion Flames" 1st Int'l. Symp on Comb., 2-12, The Combustion Institute, 1978.
65. Kim, J.S., de Ris, J., and Kroesser, F.W., "Laminar Free Convection Burning of Fuel Surfaces," 13th Int'l. Symp. on Comb., 949-961, The Combustion Institute, 1971.
66. Pagni, P.J., "Diffusion Flame Analyses," Fire Safety J., 3, 273-286, 1980/81.
67. Hertzberg, M., Cashdollar, K., Litton, C. and Burgess, D., "The Diffusion Flame in Free Convection," Report of Investigation 8263, U.S. Bureau of Mines, Washington, 1978.

68. Sibulkin, M., "Free Convection Diffusion Flames," Prog. in Energy and Comb. Sci., to appear.
69. Williams, F.A., Combustion Theory, 2nd ed., Benjamin/Cummings, Menlo Park, CA 1985.
70. Beier, R.A., Pagni, P.J., and Okoh, C.I., "Soot and Radiation in Combusting Bounding Layers," in Fire Science for Fire Safety, eds. R.S. Levine and P.J. Pagni, 235-261, Gordon and Breach, London, 1984.
71. Ang, J.A., "Perturbed Boundary Layer Diffusion Flames," doctoral dissertation, Mechanical Engineering, University of California at Berkeley, 1986.
72. Mataga, T., Ang, J.A., and Pagni, P.J., "A Two Sheet Model for Fuel Pyrolysis and Reaction," Paper No. 17, Eastern Section of the Combustion Institute-Fall Technical Meeting, 1987.
73. Spalding, D.B., Convective Mass Transfer, Arnolds Press, London, 1963.
74. Products Research Committee, "Materials Bank Compendium of Fire Property Data," NBS, Washington, February 1980.
75. Products Research Committee, "Fire Research on Cellular Plastics," NBS, Washington, April 1980.
76. Pagni, P.J., and Shih, T.M., "Excess Pyrolyzate," 16th Int'l. Symp. on Comb., 1329-1343, The Combustion Institute, 1976.
77. Beyler, C.L., "Ignition and Burning of a Layer of Incomplete Combustion Products," in Fire Science for Fire Safety, eds. R.S. Levine and P.J. Pagni, 287-303, Gordon and Breach, London, 1984.
78. Nelson, H.E., "An Engineering Analysis of the Early Stages of Fire Development-The Fire at the DuPont Plaza Hotel and Casino - 12/31/86," NBSIR 87-3560, NBS, Washington, 1987.
79. Kinoshita, C.M., and Pagni, P.J., "Laminar Wake Flame Heights," ASME J. Heat Transfer, 102:1, 104-109, 1980.
80. Shih, T.M., and Pagni, P.J., "Wake Turbulent Flames," ASME Paper No. 77-HT-97, ASME, New York, 1977.
81. Mitler, H.E., "Algorithm for the Mass-Loss Rate of Burning Wall," NBSIR 87-3682, NBS, Washington, 1987.
82. Ahmad, T., and Faeth, G.M., "Turbulent Wall Fire," 17th Int'l. Symp. on Comb., 1149-1160, The Combustion Institute, 1978.
83. Orloff, L., de Ris, J., and Markstein, G.H., "Upward Turbulent Fire Spread and Burning of Fuel Surface," 15th Int'l. Symp. on Comb., 183-192, The Combustion Institute, 1974.
84. Orloff, L., Modak, A.T., and Alpert, R.L., "Burning of Large-Scale Vertical Surfaces," 16th Int'l. Symp. on Comb., 1345-1354, The Combustion Institute, 1976.

85. Kanury, A.M., "Modeling of Pool Fires with a Variety of Polymers," 15th Int'l. Symp. on Comb., 193-202, The Combustion Institute, 1974.
86. Modak, A.T., "The Burning of Large Pool Fires," Fire Safety J., 3:3, 177-184, 1981.
87. Orloff, L., "Simplified Radiation Modeling of Pool Fires," 18th Int'l Symp. on Comb., 549-561, The Combustion Institute, 1981.
88. Orloff, L., and de Ris, J., "Froude Modeling of Pool Fires," 19th Int'l. Symp. on Comb., 885-895, The Combustion Institute, 1983.
89. Babrauskas, V., "Free Burning Fires," Fire Safety J., 11, 33-51, 1981.
90. Babrauskas, V., Lawson, J.R., Walton, W.D., and Twilley, W.H., "Upholstered Furniture Heat Release Rates Measured with a Furniture Calorimeter," NBSIR 82-2604, NBS, Washington, 1982.
91. Babrauskas, V., and Wickstrom, U., "The Rational Development of Bench Scale Fire Tests for Full Scale Fire Prediction," this Symposium.
92. Tewarson, A., "Fully Developed Enclosure Fires of Wood Cribs," 20th Int'l. Symp. on Comb., 1555-1566, The Combustion Institute, 1984.
93. The Combustion Institute, 10th Int'l. Symp. on Comb., p. 1468, 1965.
94. The Combustion Institute, 20th Int'l. Symp. on Comb., pp. 2146-2149, 1984.
95. de Ris, J., "Fire Radiation-A Review," 17th Int'l. Symp. on Comb., 1003-1016, The Combustion Institute, 1978.
96. Tien, C.L., and Lee, S.C., "Flame Radiation," Prog. Energy Comb. Sci 8, 41-59, 1982.
97. Siegel, R., and Howell, J.R., Thermal Radiation Heat Transfer, 2nd ed., Hemisphere, Washington, 1981.
98. Sparrow, E.M., and Cess, R.D., Radiation Heat Transfer, Brooks/Cole, Belmont CA, 1966.
99. Hottel, H.C., and Sarofim, A.F., Radiative Transfer, McGraw Hill, New York, 1967.
100. Markstein, G.H., "Radiant Emission and Smoke Points for Laminar Diffusion Flames of Fuel Mixtures," 21st Int'l. Symp. on Comb., 1107-1114, The Combustion Institute, 1986.
101. Brosmer, M.A., and Tien, C.L., "Radiative Energy Blockage in Large Pool Fires," Comb. Sci. and Tech., 51, 21-37, 1987.
102. Wagner, H.Gg., "Soot Formation in Combustion," 17th Int'l. Symp. on Comb., 3-19, The Combustion Institute, 1978.

103. Smyth, K.C., Miller, J.H., Dorfman, R.C., Mallard, W.G., and Santoro, R.J., "Soot Inception in a Methane/Air Diffusion Flame as Characterized by Detailed Species Profiles," Comb. and Flame, 62, 157-181, 1985.
104. Bard, S., and Pagni, P.J., "Spatial Variation in Soot Volume Fractions in Pool Fire Diffusion Flames," in Fire Safety Science - Proceedings of the First International Symposium, eds., C.E. Grant, and P.J. Pagni, 361-369, Hemisphere, New York, 1986.
105. Frenklach, M., Clary, D.W., Gardiner, W.C., Jr., and Stein, S.E., "Detailed Kinetic Modeling of Soot Formation in Shock-Tube Pyrolysis of Acetylene," 20th Int'l. Symp. on Comb., 887-901, The Combustion Institute, 1984.
106. Fernandez-Pello, A.C., and Hirano, T., "Controlling Mechanisms of Flame Spread," Fire Sci. and Tech., 2, 17-54, 1982.
107. Williams, F.A., "Mechanisms of Fire Spread," 16th Int'l. Symp. on Comb., 1281-1294, The Combustion Institute, 1976.
108. Glassman, I., and Dryer, F.L., "Flame Spreading Across Liquid Fuels," Fire Safety J., 3, 123-138, 1980/81.
109. Akita, K., "Some Problems of Flame Spread Along a Liquid Surface," 14th Int'l. Symp. on Comb., 1075-1083, The Combustion Institute, 1973.
110. Quintiere, J., "A Simplified Theory for Generalizing Results from a Radiant Panel Rate of Flame Spread Apparatus," Fire and Materials, 5:2, 52-60, 1981.
111. Dosanjh, S.S., Pagni, P.J., and Fernandez-Pello, A.C., "Forced Cocurrent Smoldering Combustion," Comb. and Flame, 68, 131-142, 1987.
112. Ohlemiller, T.J., "Modeling of Smoldering Combustion Propagation," Prog. Energy Comb. Sci., 11, 277-310, 1986.
113. Strehlow, R.A., and Baker, W.E., "The Characterization and Evaluation of Accidental Explosions," Prog. Energy Comb. Sci., 2:1, 27-60, 1976.
114. NACA, Basic Considerations in the Combustion of Hydrocarbon Fuels with Air, eds. H.C. Barnett, and R.R. Hibbard, NACA Report 1300, U.S. Govt. Print. Off., Washington, 1958.
115. Friedman, R., "Quantification of Threat from a Rapidly Growing Fire in Terms of Relative Material Properties," Fire and Materials, 2:1, 27-33, 1978.
116. Alpert, R.L., and Ward, E.J., "Evaluation of Unsprinklered Fire Hazards," Fire Safety J., 7, 127-143, 1984.
117. Cooper, L.Y., and Stroup, D.W., "ASET-A Computer Program for Calculating Available Safe Egress Time," Fire Safety J., 9, 29-45, 1985.

118. Jones, W.W., "A Review of Compartment Fire Models," NBSIR 83-2684, NBS, Washington, 1983.
119. Mitler, H.E., and Rockett, J.A., "How Accurate is Mathematical Fire Modeling?" NBSIR 86-3459, NBS, Washington, 1987.
120. Stroup, D.W., "A Catalog of Compartment Fire Model Algorithms and Associated Computer Subroutines," NBSIR 87-3607, NBS, Washington, 1987.
121. Quintiere, J., "The Spread of Fire from a Compartment-A Review," in Design of Buildings for Fire Safety, STP 685, eds. E.E. Smith and T.Z. Harmathy, 139-168, ASTM, Philadelphia, 1980.
122. Emmons, H.W., "The Calculation of a Fire in a Large Building," ASME Paper No. 81-HT-2, ASME, New York, 1981.
123. Mitler, H.E., and Rockett, J.A., "Users' Guide to FIRST, A Comprehensive Single-Room Fire Model," NBSIR 87-3595, NBS, Washington, 1987.
124. Levine, R.S., Memoranda to the Ad Hoc Mathematical Fire Modeling Working Group, NBS, Washington, 1978 et seq.
125. Seader, J.D., and Einhorn, I.N., "Some Physical, Chemical, Toxicological and Physiological Aspects of Fire Smokes," 16th Int'l. Symp. on Comb., 1423-1445, The Combustion Institute, 1976.
126. Quintiere, J., "Growth of Fire in Building Compartments," in Fire Standards and Safety, STP 614, ed. A.F. Robertson, 131-167, ASTM, Philadelphia, 1977.
127. Thomas, P.H., Bullen, M.L., Quintiere, J.G., and McCaffrey, B.J., "Flashover and Instabilities in Fire Behavior," Comb. and Flame, 38, 159-171, 1980.
128. Thomas, P.H., "Fires and Flashover in Rooms-A Simplified Theory," Fire Safety J., 3, 67-76, 1980/81.
129. Yang, K.T., Lloyd, J.R., Kanury, A.M., and Satoh, K., "Modeling of Turbulent Buoyant Flows in Aircraft Cabins," in Fire Science for Fire Safety, eds., R.S. Levine and P.J. Pagni, 107-118, Gordon and Breach, London, 1984.
130. Cox, G., Kumar, S., and Markafos, N.C., "Some Field Model Validation Studies," in Fire Safety Science-Proceedings of the First International Symposium, eds., C.E. Grant and P.J. Pagni, 159-171, Hemisphere, New York, 1986.
131. Liebowitz, H., Fracture, 7, p. 27, Academic Press, New York, 1972.
132. Bansal, N.P., and Dorems, R.H., Handbook of Glass Properties, Academic Press, New York, 1986.
133. Finnie, I., private communication, 1988.
134. Emmons, H.W., "Why Fire Model? The MGM Fire and Toxicity Testing," Fire Safety Journal, 13, 77-85, 1988.